## ARA

NEW SPECIMEN PAPERS
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## GCSE <br> Mathematics <br> Specification (8300/1F)

## Paper 1 Foundation tier

Date
Morning
1 hour 30 minutes

## Materials

| For this paper you must have: |  |
| :--- | :--- |
| $\bullet \quad$ mathematical instruments |  |
| You must not use a calculator |  |

Model
Solutions

## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the bottom of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book.
- In all calculations, show clearly how you work out your answer.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper.

These must be tagged securely to this answer book.

[^0]1 How many centimetres are there in 3.7 metres? Circle your answer.

| 0.037 | 0.37 |
| :--- | :--- |
| $3.7 \mathrm{~m} \xrightarrow[\times 100]{ } 370 \mathrm{~cm}$ |  |

2 Which of these is the net of a cube?
Circle the correct letter.

A

(c)


B


D


3 Circle the fraction that is not equivalent to $\frac{3}{8}$
$\frac{6}{16}$
$\frac{9}{24}$
$\frac{12}{32}$
$\stackrel{\text { 총 }}{\sim}$

$$
\frac{15}{35}=\frac{3}{7} \operatorname{not} \frac{3}{8}
$$


$4 \quad$ Simplify $\quad 5 a-(2 a+6)$
Circle your answer.

$$
3 a+6
$$

$$
9 a
$$

$$
-3 a
$$

$3 a-6$
$5 a-(2 a+6)$
$=5 a-2 a-6$
$=3 a-6$

Turn over for the next question

5 Complete the table.
[2 marks]

| Minutes | Hours |
| :---: | :---: |
| 30 | $\frac{1}{2}$ |
| 40 | $\frac{2}{3}$ |
| 135 | $2 \frac{1}{4}$ |

$$
\begin{aligned}
& \frac{40}{60}=\frac{4}{6}=\frac{2}{3} \\
& 21 / 4=2.25 \\
& 2.25 \times 60= \\
& (2 \times 60)+(0.25 \times 60)= \\
& 120+15=135 \text { minutes }
\end{aligned}
$$

6 Here are some numbers.
9.6
12.6
15.4
7.6
12.4
17.4

Write the numbers in pairs so that the sum of the numbers in each pair is the same.
[2 marks]

$$
\frac{9.6+12.6+15.4+7.6+12.4+17.4}{3}=\frac{75}{3}=25
$$

So each pair adds to 25.
$7.6+17.4=25$
$9.6+15.4=25$
$12.4+12.6=25$
Answer 7.6 and 17.4

| 9.6 | and 15.4 |
| :--- | :--- | :--- |
| 12.4 | and 12.6 |

7 This triangle is drawn accurately.


What type of triangle is it?
Tick two boxes.
acute-angled
obtuse-angled

equilateral

isosceles

scalene


Turn over for the next question
$8 \quad$ Work out $51 \%$ of 400

So (50.t of 400$)+(1.100+400)$
$200+4=204$

Answer 204
$9 \quad$ Write 180 g as a fraction of 3 kg
Give your answer in its simplest form.
$3 \mathrm{~kg}=3000 \mathrm{grams}$
$\frac{1809}{30009}=\frac{18}{300}=\frac{6}{100}=\frac{3}{50}$

10 Here are some properties of numbers.
A Even
B Odd
C Prime
D Square
E Two-digit

10 (a) Which two properties does the number 4 have?
Circle the correct letters.
[1 mark]
(A)
B
C
(D)
E
$2 \times 2=4$
$\sqrt{4}=2$

10 (b) Can one number have all of the properties?
Tick a box.


Give a reason for your answer.

## A number cont be odd and even at the same time.

10 (c) Write down a number with three of the properties.
State which properties it has.
$\stackrel{16}{\underline{1}}$
Even $\rightarrow 2 \times 8=16$
Square $\rightarrow \sqrt{16}=4$
2 digits $\rightarrow \mathbf{6}$
Number
16

Properties A , D E $\qquad$

11 Ranjit has six coins in his pocket.
If he picks five of the coins
the most he could pick is $£ 4.60$
the least he could pick is $£ 2.70$
How much money does he have altogether?
$S$ coins
To mater $\in 4.60 \rightarrow \epsilon 2, \in 2,20 p, 20 p, 20 p$ 5 coins
To make $t 2.70 \rightarrow \sqrt{\epsilon 2,20 p, 20 p, 20 p, 10 p}$

So 6 coins he has is $\in 2, \in 2,20 p, 20 p, 20 p, 10 p$,
$\qquad$ (
$\qquad$

Answer £ 4-70

12 Here are three expressions.
$\frac{b}{a}$
$a-b$
$a b$

When $a=2$ and $b=-6$ which expression has the smallest value? You must show your working.

$$
\begin{aligned}
& \frac{b}{a} \rightarrow \frac{-6}{2}=-3 \\
& a-6 \rightarrow 2--6=2+6=8
\end{aligned}
$$

$$
a b \rightarrow 2 x-6=-12=\text { smallest }
$$

Answer $a b$

## Turn over for the next question

13 The table shows the ratio of teachers to children needed for two activities.

|  | teachers children |
| :--- | ---: |
| Climbing | $1: 4$ |
| Walking | $1: 9$ |

13 (a) There are 7 teachers to take children climbing.
What is the greatest number of children that can go climbing?

$$
\begin{aligned}
& T: C \quad \times 7 \quad T: c \\
& 1: 4 \xrightarrow{T}: 28 \\
& \hline
\end{aligned}
$$

Answer 28

13 (b) 49 children want to go walking.
What is the smallest number of teachers needed?
T: C
[1 mark]

Answer 6
5 teachers con take 45 children so we reed 6 kachers for 49 .
$14 \quad$ Shape $R$ is a rectangle.
A smaller rectangle is cut from $R$ to form shape $L$.
Not drawn accurately


Which one of these statements is true?
Tick a box.

The perimeter of $R$ is longer than the perimeter of $L$

The perimeter of $R$ is the same as the perimeter of $L$

The perimeter of $R$ is shorter than the perimeter of $L$


It is not possible to tell which perimeter is longer

Turn over for the next question

15 Textbooks are stored on two shelves.
Each shelf is 0.72 metres long.
Each textbook is 30 millimetres wide.
Not drawn accurately


Can 50 textbooks be stored on these shelves?
You must show your working.


Two shelves total leyth $\rightarrow 0.72+0.72=1.44 \mathrm{~m}=144 \mathrm{~cm}=1440 \mathrm{~mm}$

$$
\frac{1440}{30}=\frac{144}{3} \rightarrow \frac{120}{3}+\frac{24}{3}=40+8=48 \text { books can fit only. }
$$

Answer No, only 48 can fit.

16 All tickets for a concert are the same price.
Amy and Dan pay $£ 63$ altogether for some tickets.
Amy pays $£ 24.50$ for 7 tickets.
How many tickets does Dan buy?

$$
\frac{\epsilon 24 \cdot 50}{7}=1 \text { ticket price }=7 \sqrt{24.3 .50}=63.50 \text { per ticket }
$$

$$
\epsilon 63-624.50=638.50
$$

$$
\frac { \epsilon 3 8 . 5 0 } { \epsilon 3 . 5 0 } \rightarrow 3 5 \longdiv { 0 1 1 } \frac { 3 8 ^ { 3 } 5 } { 0 } = 1 1 \text { tickets }
$$



17 (a) On the same grid, draw the graph of $y=x+1$ for values of $x$ from 0 to 5

17 (b) Use the graphs to solve the simultaneous equations

$$
y=5-x \text { and } y=x+1
$$

## point where lines inter sect

$(2,3)$
So $\begin{aligned} & x=2 \\ & y=3\end{aligned}$

$$
x=\mathbf{2}
$$

$$
y=3
$$

18 The table shows the sales of food and drink for three days at a market stall.

| Day | Sales of food (£) | Sales of drink (£) |
| :--- | :---: | :---: |
| Thursday | 34 | 16 |
| Friday | 22 | 48 |
| Saturday | 46 | 28 |

Hannah uses this information to draw a composite bar chart.

Sales of food and drink


Write down three different mistakes that she has made.

Mistake 1 There is no key

Mistake 2 Friday should reach $\leqslant 70$

Mistake 3 Saturdays bars are wrong way around

19 Sam wants to buy a camera for $£ 345$
He has already saved $£ 96$
Each week
his pay is $£ 80$
he saves $30 \%$ of this pay.
How many more weeks must he save?
[4 marks]

$$
\begin{aligned}
& E 345-\angle 46=E 249 \text { left to save } \\
& \text { saves } 30.1 \text { of } \epsilon 80 \text { each week } \rightarrow 0.3 \times \angle 80=3 \times 8=E 24 \\
& \frac{\epsilon 249}{\epsilon 24}=\frac{\epsilon 240}{\epsilon 24}+\frac{\epsilon 9}{\epsilon 24}=10 \text {. Something } \\
& \text { So reeds } 11 \text { weeks }
\end{aligned}
$$

[^1]20 (a) $w$ and $x$ are whole numbers.

$$
\begin{aligned}
& w>40 \\
& x<30
\end{aligned}
$$

Work out the smallest possible value of $w-x$

$$
\begin{aligned}
& \text { Smaller } w \text { - lorgest } x \\
& 41-29=12
\end{aligned}
$$

Answer 12

20 (b) $y$ and $z$ are whole numbers.

$$
\begin{aligned}
& y<60 \\
& z \leqslant 50
\end{aligned}
$$

Work out the largest possible value of $y+z$

Largest $y+$ Largest $z$

$$
59+50=109
$$

$\qquad$

21 (a) Work out $2.4 \times 0.002$
$2.4 \times 0.002=24 \times 0.0002$
$=0.0048$
Answer 0.0048

21 (b) Write $1.2 \times 10^{-5}$ as an ordinary number.


Answer 0.000012

21 (c) Write 2500000 in standard form.


Answer $\quad 2.5 \times 10^{6}$

Turn over for the next question

22 The diagram shows information about the scores of Class 3 A in a spelling test.


22 (a) A student is chosen at random from Class 3 A .
Work out the probability that the student's score was the mode for the class.

Mode $=$ most $=8$ score
$\frac{\text { people with } 8 \text { score }}{\text { All students }} \rightarrow \frac{9}{2+3+6+7+9}=\frac{9}{27}=\frac{1}{3}$ Answer 1/3

The diagram shows information about the scores of Class 3B in the same test.

## Class 3B



22 (b) Show that Class 3A had more consistent scores than Class 3B.
Use the data from both diagrams.

Rarge of Class $3 \mathrm{~A} \rightarrow 8-4=4$
Renge of class $3 B \rightarrow 8-3=5$
3A has smallu rorge so their scores are more consistent.

22 (c) Lucy is one of the 29 students in Class 3B.
Her score was the same as the median score for her class.
Work out her score.
Number of students $\longrightarrow 2+2+4+7+8+6=29$
Meelian position $=\frac{29+1}{2}=15^{\text {th }}$ position
isth value $=6$
Answer 6

23 Kelly is trying to work out the two values of $w$ for which $3 w-w^{3}=2$
Her values are 1 and -1

Are her values correct?
You must show your working.
$1 \rightarrow 3 w-w^{3}=2 \rightarrow 3(1)-(1)^{3}=3-1=2$
$-1 \rightarrow 3 w-w^{3}=2 \rightarrow 3(-1)-(-1)^{3}=-3--1=\underline{\underline{-2}}$

## $x$

## Only correct answer is $w=1$

24 The diagram shows a semicircle of radius 8 cm


Work out the area of the semicircle.
Give your answer in terms of $\pi$.

$$
\begin{aligned}
1 / 2 \pi r^{2} \rightarrow 1 / 2 \pi(8)^{2} & =1 / 2 \times 64 \pi \\
& =32 \pi \mathrm{~cm}^{2}
\end{aligned}
$$

Answer
$32 \pi$
$\mathrm{cm}^{2}$

25 Work out $2 \frac{3}{4} \times 1 \frac{5}{7}$

Give your answer as a mixed number in its simplest form.

$$
2 \frac{3}{4} \rightarrow \frac{11}{4} \quad 1 \frac{5}{7} \rightarrow \frac{12}{7}
$$

$$
\begin{aligned}
& \frac{11}{4} \times \frac{12}{7}=\frac{132}{28}=\frac{66}{14}=\frac{33}{7} \\
& \frac{33}{7}=\frac{28}{7}+\frac{5}{7}=4 \frac{5}{7}
\end{aligned}
$$

$$
5 x-2>3 x+11
$$

$$
2 x>13
$$

$$
x>13 / 2
$$

$$
x>6.5
$$

Answer $x>6.5$

Turn over for the next question

27 The $n$th term of a sequence is $2 n+1$
The $n$th term of a different sequence is $3 n-1$
Work out the three numbers that are
in both sequences
and
between 20 and 40

Sequance $1 \rightarrow 21,23,25,27,29,31,33,35,37,39$
sequence $2 \rightarrow 20,23,26,29,32,35,38$

23,29 and 35
Answer 23 29
35

28 White paint costs $£ 2.80$ per litre.
Blue paint costs $£ 3.50$ per litre.
White paint and blue paint are mixed in the ratio $3: 2$
Work out the cost of 18 litres of the mixture.
[4 marks]
$w: B$
$3: 2 \rightarrow$ Total $3+2=5$ parts of 18 Litres
$\frac{18}{5}=\frac{36}{10}=3.6$ litre per port

```
    W:B
3\times3.6L:2\times3.6L
    10.8L:7.2L
```

    White paint cost \(\rightarrow 10.8 \times 62.80=(10 \times 2.8)+(0.8 \times 2)+(0.8 \times 0.8)\)
                        \(28+1.6+0.64\)
                \(=\epsilon 28+2.24=\epsilon-30.24\)
    Blue paint cost $\rightarrow 7.2 \times 3.5=(7 \times 3)+(0.2 \times 3)+(7.2 \times 0.5)$
$21+0.6+3.6$
$=21+4.2=\underline{E} 25.20$
Total cost $\rightarrow 30.24+25-20$
$=t 55.44$
Answer $£ \quad 55.44$

Turn over for the next question

29 Here are sketches of four triangles.


In each triangle
the longest side is exactly 1 cm
the other length is given to 2 decimal places.
29 (a) Circle the value of $\cos 50^{\circ}$ to 2 decimal places.
0.77
0.53
0.64
0.86

Use $\rightarrow$


$$
\cos =C A n
$$

$$
\cos 50=\frac{0.64}{1}=0.64
$$

29 (b) Work out the value of $x$.
Give your answer to 1 decimal place.


Not drawn accurately
[2 marks]
$\cos 50=\frac{\text { adjacent }}{\text { hypotenuse }}=\frac{x}{4}$

$$
\begin{aligned}
& 0.64=\frac{x}{4} \rightarrow 0.64 \times 4=x \\
&(0.60 \times 4)+(0.04 \times 4) \\
& 2.4+0.16=2.56 \\
&=2.6
\end{aligned}
$$

Turn over for the next question
$30 \quad A B C H$ is a square.
HCFG is a rectangle.
$C D E F$ is a square.
They are joined to make an L-shape.


Show that the total area of the L-shape, in $\mathrm{cm}^{2}$, is $x^{2}+9 x+27$

Area ABCH $\rightarrow(x+3)(x+3)=x^{2}+6 x+9$

Area $H$ MFG $\rightarrow 3(x+3)=3 x+9$

Area CDEF $\rightarrow 3 \times 3=9 \mathrm{~cm}^{2}$
$\begin{aligned} \text { Total area } & \rightarrow x^{2}+6 x+9+3 x+9+9 \\ & =x^{2}+9 x+27\end{aligned}$

## END OF QUESTIONS


[^0]:    Please write clearly, in block capitals, to allow character computer recognition.
    Centre number $\square$ Candidate number $\square$
    Surname $\square$
    Forename (s) $\square$

    Candidate signature $\qquad$

[^1]:    Answer II
    weeks

